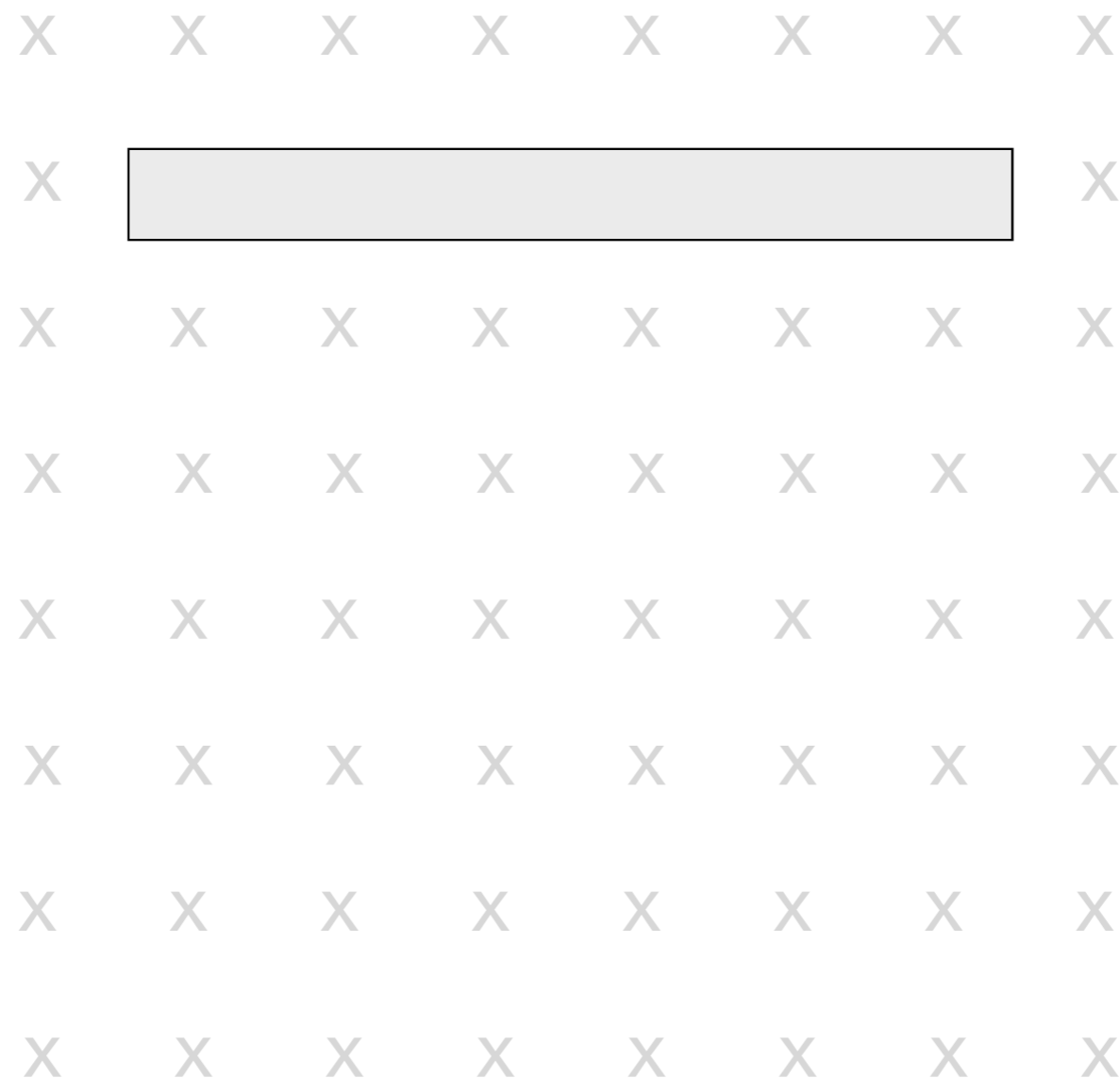


Electromagnetic induction

- Voltage across a moving rod
- Induced current - opposes changing flux
- Magnetic flux
- Lenz's law
- Induced EMF
- EMF calculations
- EMF vs flux graphs
- AC generator (alternator)

Voltage across a moving rod

- Recall the force on a charged particle moving through a field.
- A rod moving in a magnetic field will have a separation of charge along its length (or width).
- By the right-hand slap rule, + charge will be pushed to the right here.



Magnitude of induced voltage

- eg a 1m rod moving at 1m/s in Earth's field $\sim 10^{-5}\text{T}$

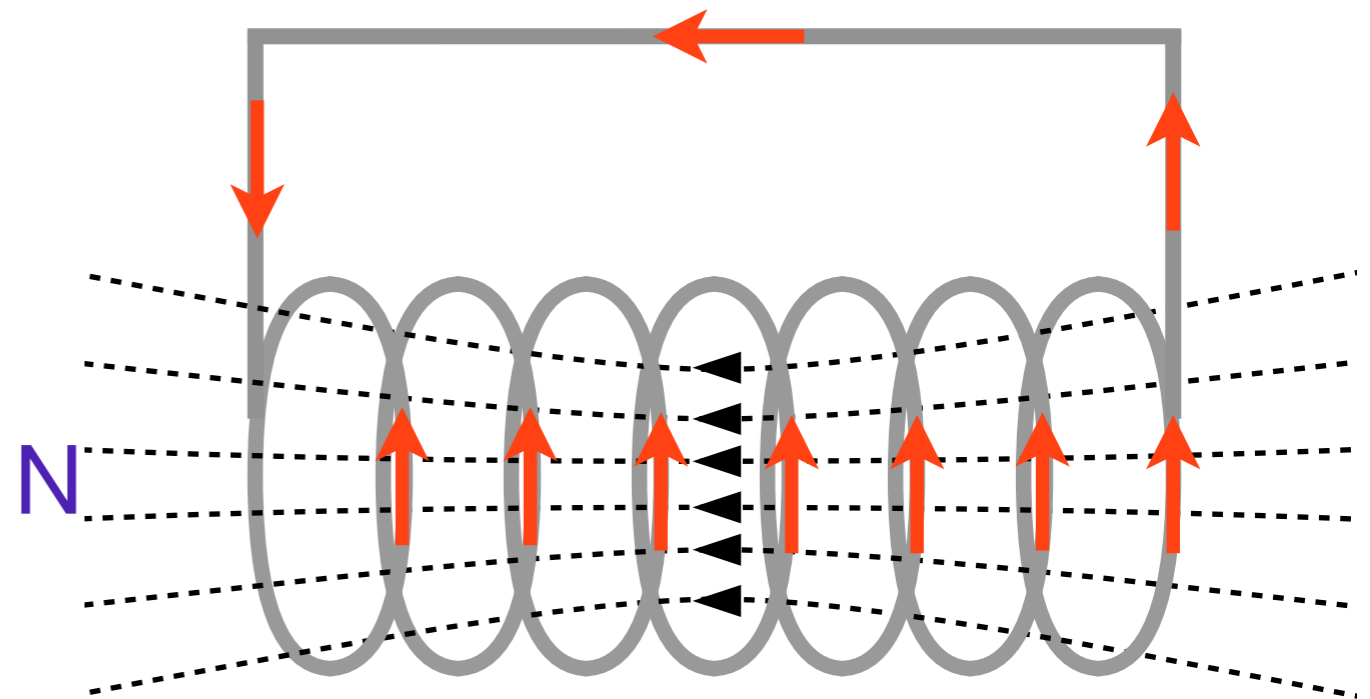
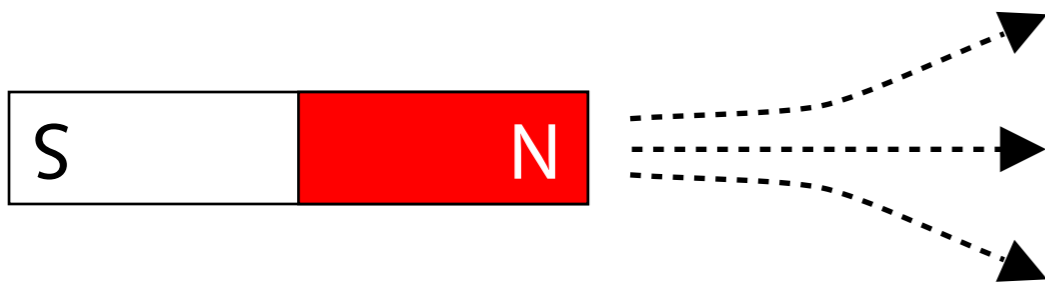
$$\begin{array}{c} F = qvB \\ \downarrow \\ W = Fx = qvBL \\ \downarrow \\ V = \frac{W}{q} = \frac{qvBL}{q} = BLv \end{array}$$

$$V = BLv = (10^{-5}\text{T})(1\text{m})(1\text{m/s})$$

$$V = 0.01\text{mV}$$

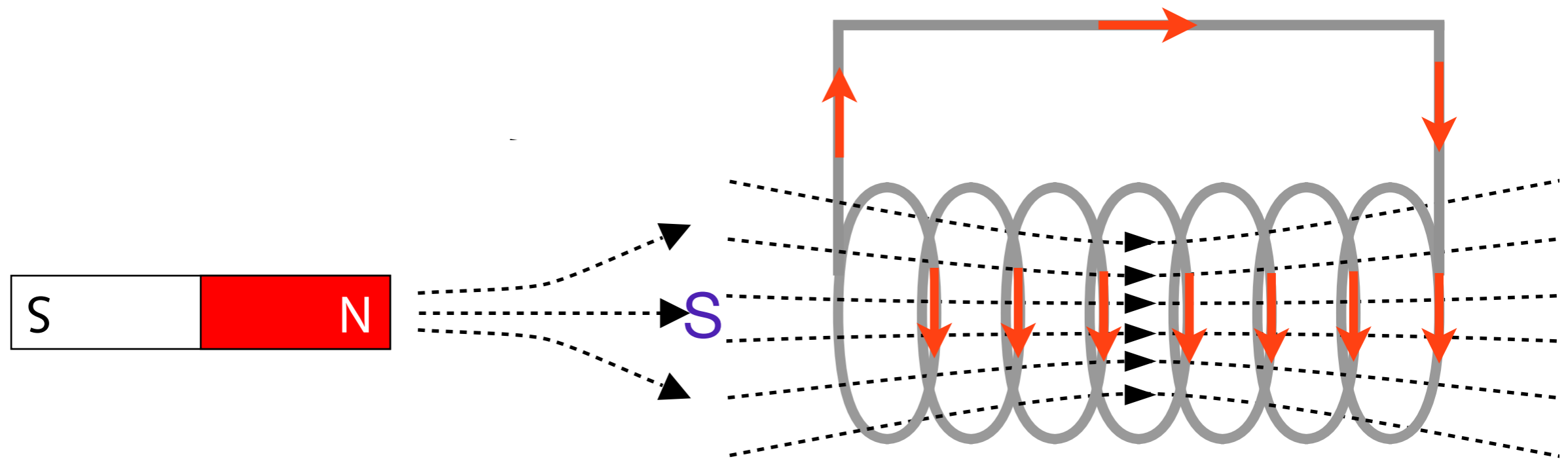
Induced current - opposes changing flux

- Pushing the north pole into a solenoid will induce a current that makes a north pole to oppose the magnet going in.



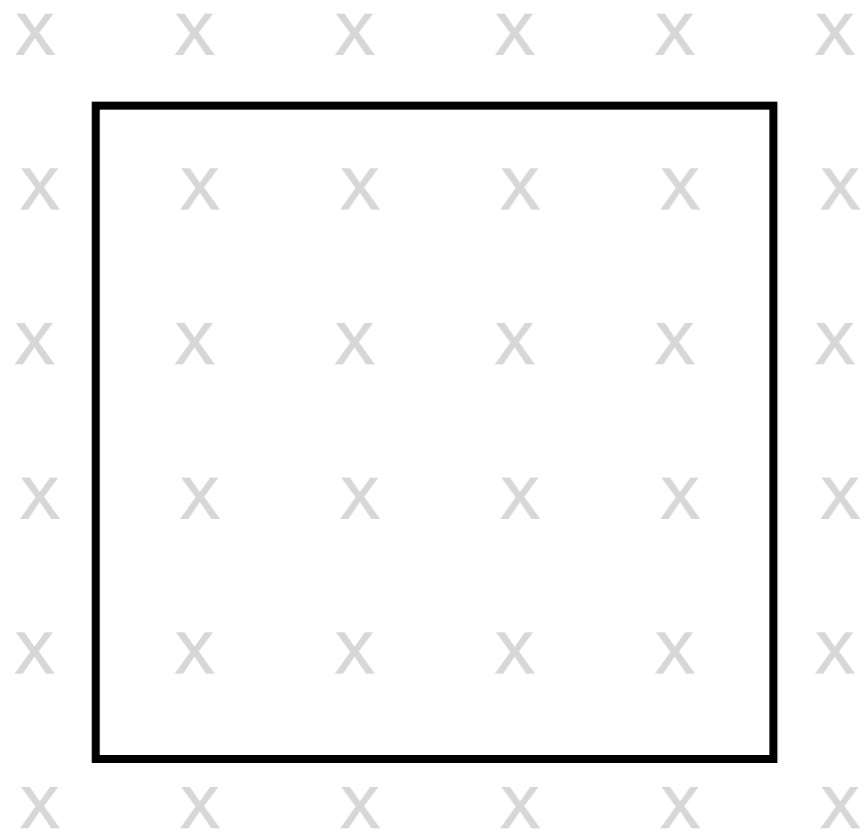
Induced current - opposes changing flux

- Pulling the north pole out of a solenoid will induce a current that makes a south pole to oppose the magnet going out.



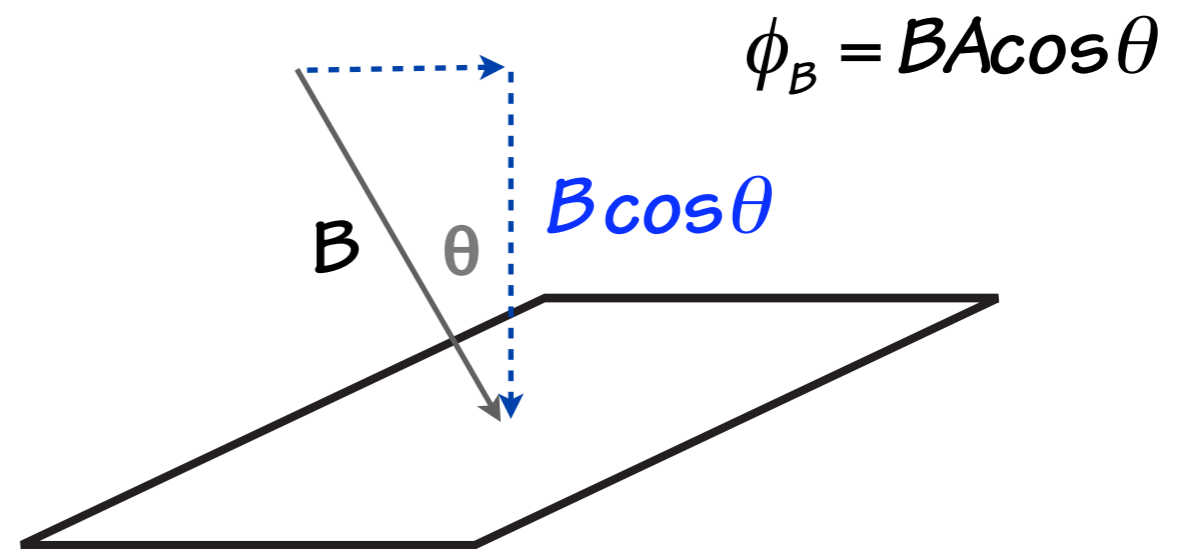
Magnetic flux

- Magnetic flux (Φ_B) is a measure of the number of field lines that pass through an area.
- $\Phi_B = B A$, Unit = Tm^2 (Weber, Wb)
- eg 20 cm x 20 cm square, 0.1 T magnetic field



$$\Phi_B = (0.2\text{m})^2 \times (0.1\text{T})$$

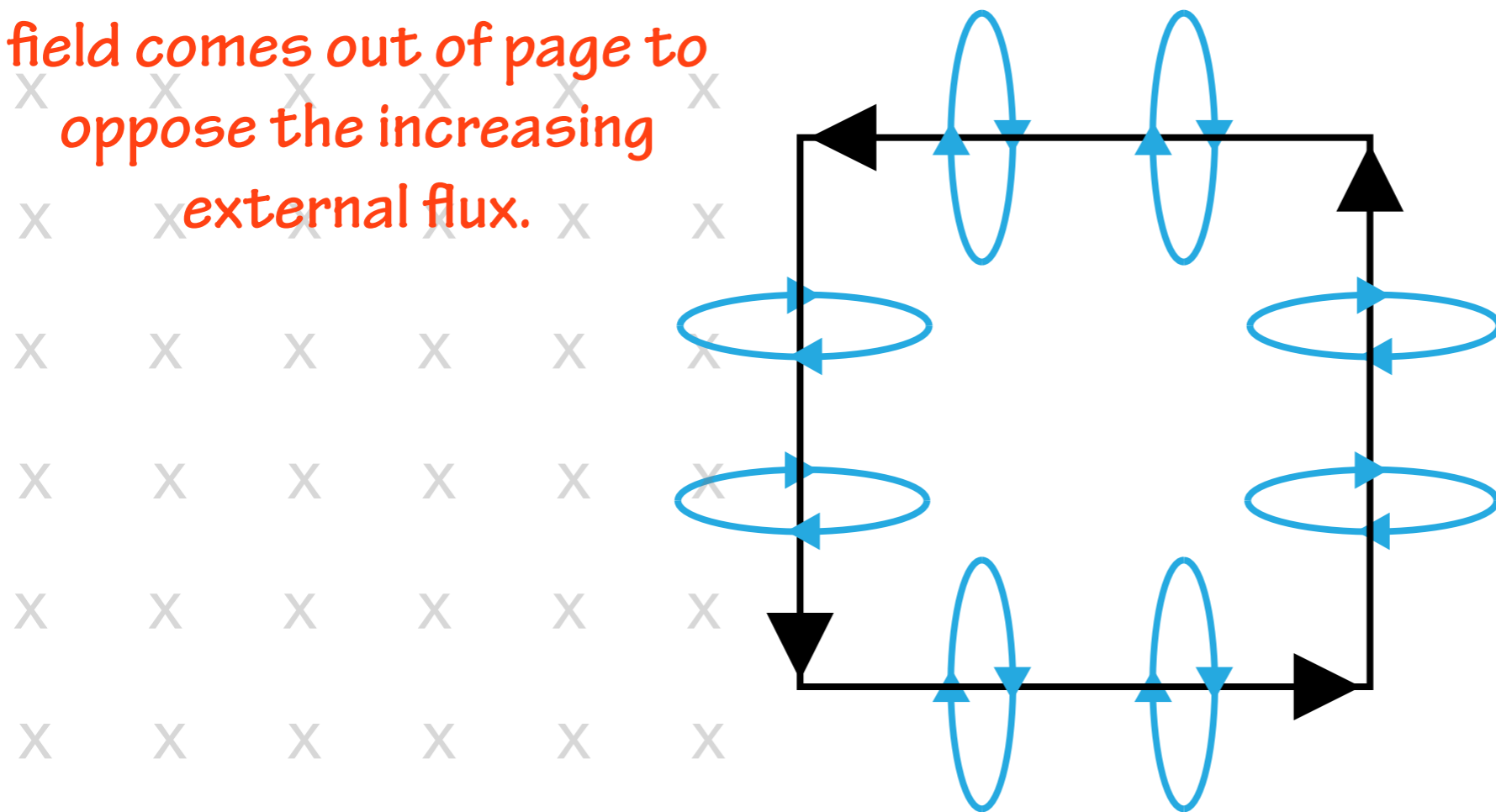
$$\Phi_B = 0.004\text{Wb}$$



Changing magnetic flux

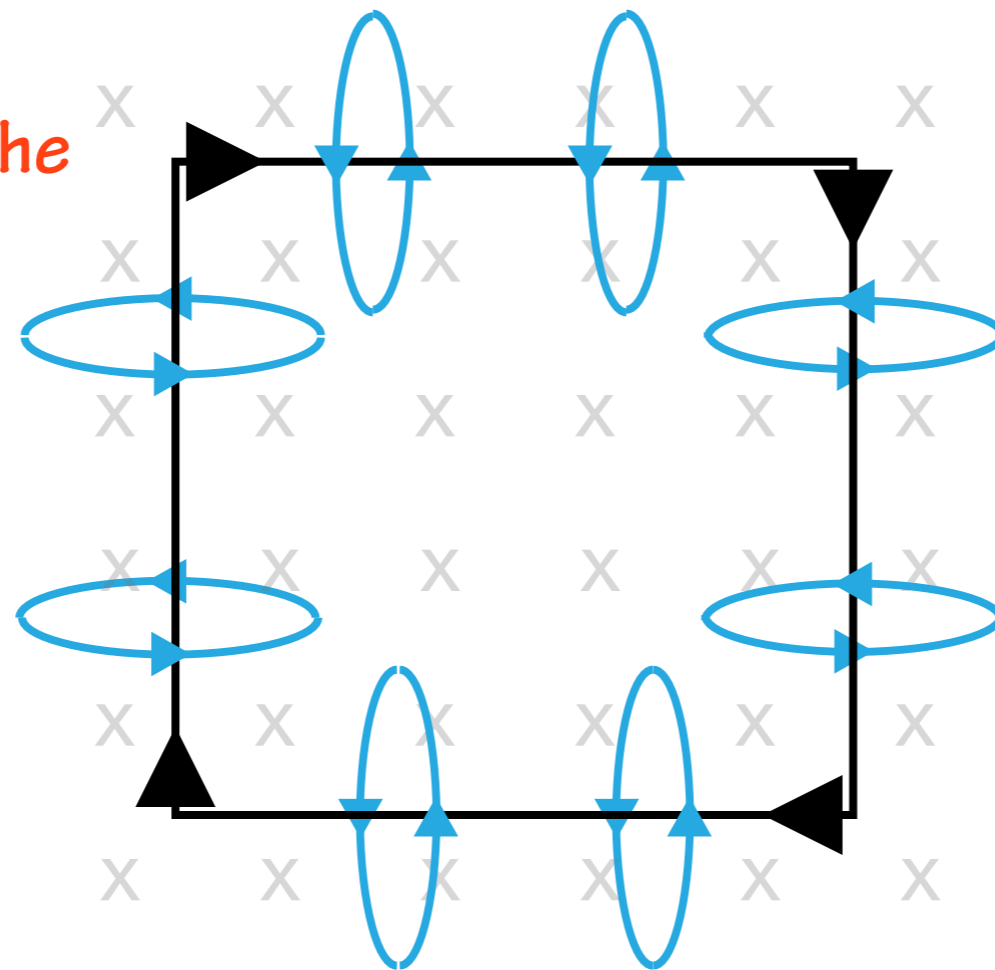
- Changes to magnetic flux induce currents.

Induced current - magnetic field comes out of page to oppose the increasing external flux.



Magnetic flux

Induced current - magnetic field goes into page to oppose the decrease of the external flux.



Lenz's law

- Faradays law: "The EMF is produced that is proportional to the rate of change of magnetic flux."
- Lenz's law: " The induced current produces its own magnetic field to oppose changes to magnetic flux. "

Magnitude of induced EMF (V) →

$$EMF = - \frac{n \Delta \phi_B}{\Delta t}$$

Number of turns of wire

Change in flux (Wb) per time (s)

Negative sign:
induced current
opposes change
in flux

Induced EMF

Voltage can be induced by:

- changing field strength.
- changing area of wire.
- changing direction of field / wire orientation.

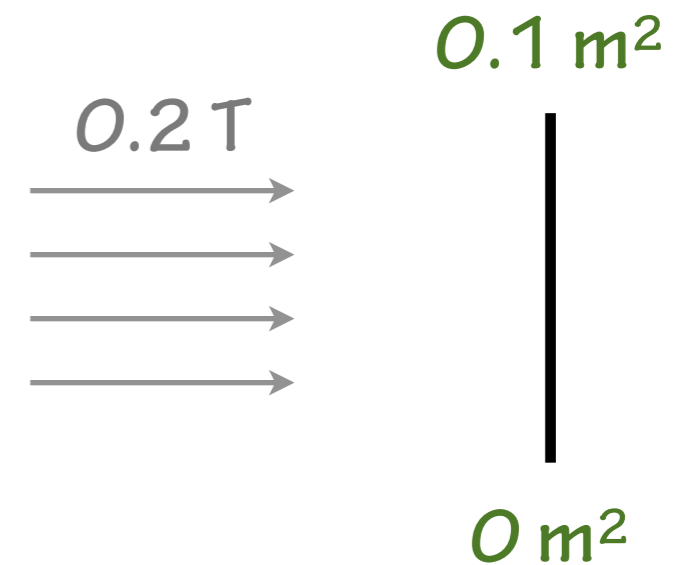
Higher EMF (voltage) from:

- stronger magnetic field.
- faster movement.
- greater area.
- multiple loops (n).

EMF calculations

- A wire loop with 100 turns of wire & an area of 0.1 m^2 is rotated through a field of 0.2 T at a rate of 5 Hz .

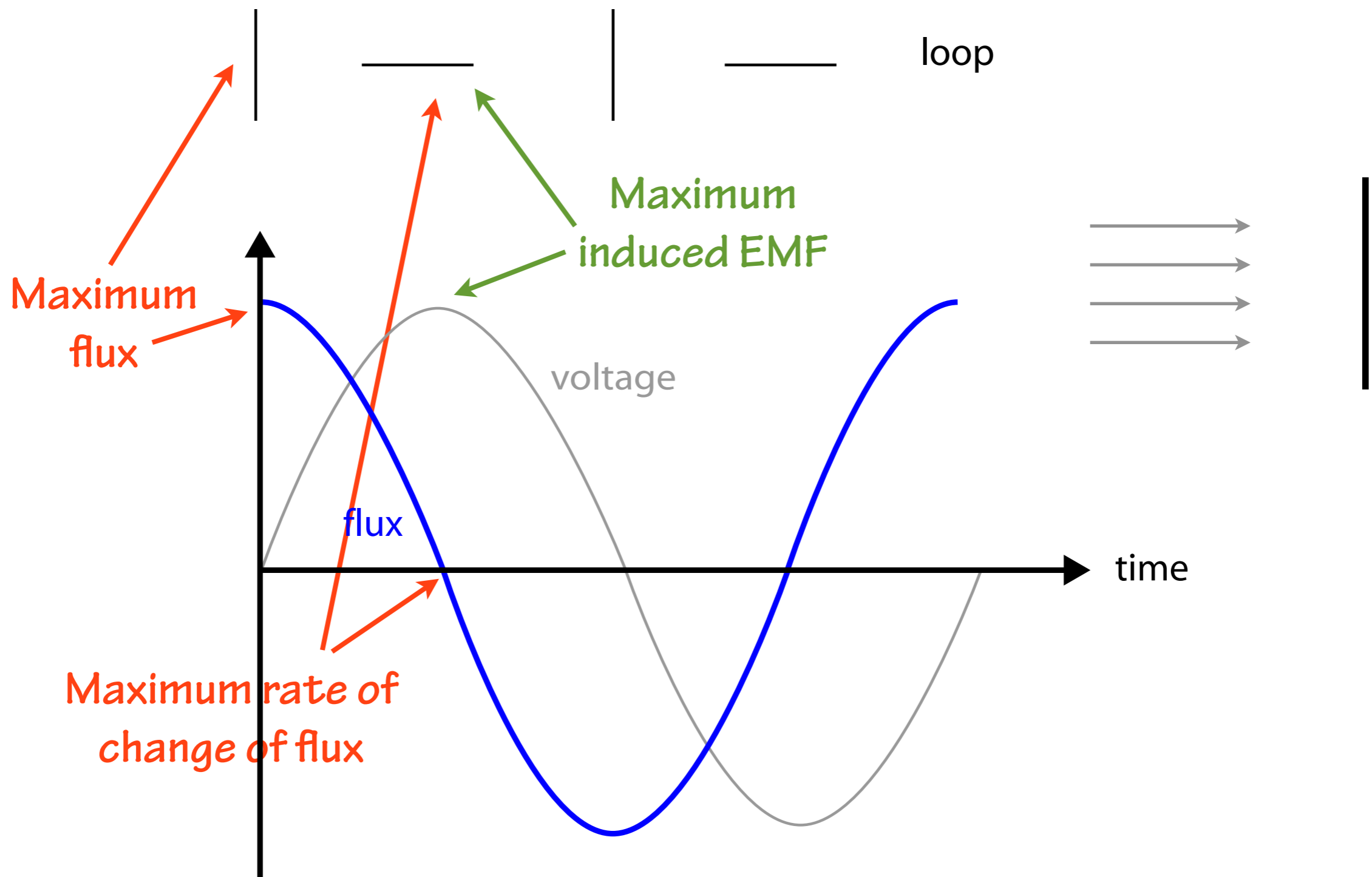
- The magnitude of B changes from $+0.2 \text{ T}$ to 0.0 T
- This takes a time of $0.25 \times 0.20 \text{ s} = 0.05 \text{ s}$



$$EMF = -\frac{n\Delta\phi_B}{\Delta t} = -\frac{100 \times (-0.2 \text{ T})(0.1 \text{ m}^2)}{0.05 \text{ s}}$$

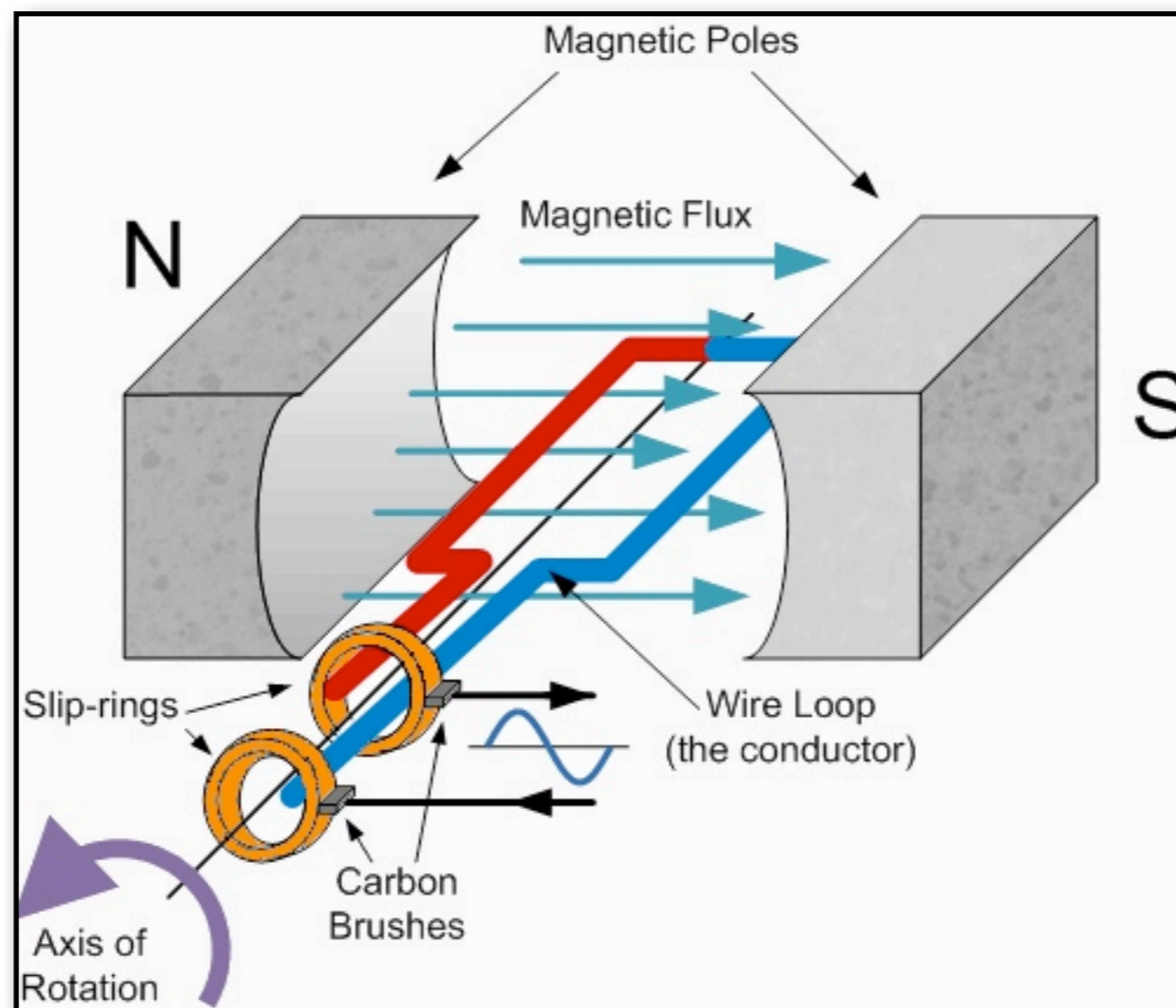
$$EMF = 40 \text{ V}$$

EMF vs flux graphs



AC generator (alternator)

- Contact is at slip rings - one side is always in contact with the same ring.
- The direction of the current & voltage will alternate every half cycle.
- Doubling rate of revolution doubles frequency and voltage.



<http://www.electronics-tutorials.ws/accircuits/sinusoidal-waveform.html>



Generator